Medical Imaging (EL582/BE620/GA4426)

Ultrasound Imaging - Lecture 2

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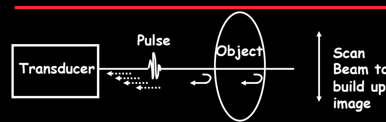
Reference

Prince and Links, Medical Imaging Signals and Systems (2nd Ed), Chap. 11

Pulse-Echo Ultrasound Imaging



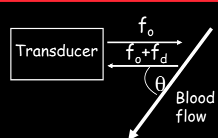
Important properties of ultrasound for imaging:

- Propagation of ultrasound in tissues (speed of sound, c)
- Reflection of ultrasound from interfaces (acoustic impedance, Z)
- Attenuation of ultrasound during propagation (α ~ 1dB/cm/MHz)

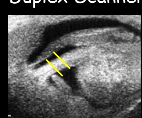
Doppler Ultrasound

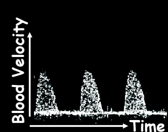
- Doppler Equation:

$$\boxed{f_d = 2f_o.v.\cos\theta/c}$$



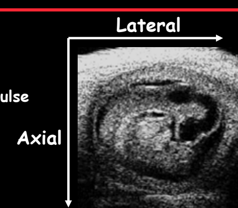
Duplex Scanner





Resolution in Ultrasound Imaging

- Axial Resolution:
  - Resolution in propagation direction
  - Determined by length of pulse propagating in tissue
- Lateral Resolution:
  - Resolution orthogonal to propagation direction
  - Determined by focusing properties of transducer



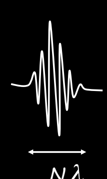
Axial Resolution

- Axial Resolution:

  Axial Resolution

  = pulse width (s) x speed of sound (m/s) /2

  = N λ/2



Lateral Resolution

- Lateral Resolution:

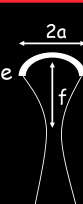
  f-number = focal length/aperture

  = f/2a

  Lateral Resolution

  = wavelength x f-number

  = λf/2a



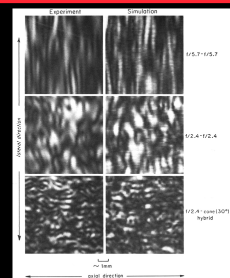
(Lateral resolution can also be limited by scan line density)

Resolution *vs* Penetration

- Resolution (axial and lateral)↑ with ↑frequency
- Penetration↓ with ↑frequency

Compromise between resolution and penetration

Ultrasound Images: Speckle



From: D Foster *et al,* Ultrasonic Imaging, 1983

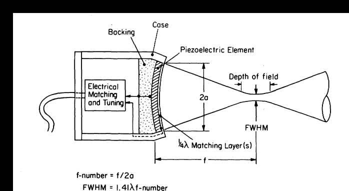
Ultrasound Images: Speckle

- Ultrasound signal is the sum of many scattering events / reflections
- Amplitude (A) of a distribution of N vibrations with phases uniformly distributed between 0 and 2π has the probability density function:

  $pdf(A) = (2A/N) \exp(-A^2/N)$ (Rayleigh, 1880)

- Mean value of this distribution (="Speckle Signal"):
  $[A] = \sqrt{(\pi[A^2]/4)}$
- "Speckle noise", the rms deviation from the mean:
  $\sqrt{([A^2]-[A])} = \sqrt{\{(1-\pi/4)[A^2]\}}$
- Inherent speckle SNR:
  $SNR = \sqrt{\{(\pi/4)/(1-\pi/4)\}} = 1.91$ (!)

Single Element Transducer



From: Hunt *et al,* IEEE Trans BME, 1983

Functions of the transducer

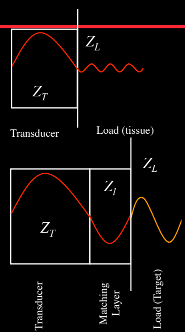
- Used both as Transmitter And Receiver
- Transmission mode: converts an oscillating voltage into mechanical vibrations, which causes a series of pressure waves into the body
- Receiving mode: converts backscattered pressure waves into electrical signals

Piezoelectric Material

- Converts electrical voltage to mechanical vibration and vice versa
- The thickness of the crystal varies with the applied voltage
- When an AC voltage is applied across the crystal, the thickness oscillates at the same frequency of the voltage
- Examples of piezoelectric Materials:
  - Crystalline (quartz), Ceramic (PZT, lead zirconium titanate), Polymers (PVDF), Composite materials
  - PZT is one of the most efficient materials
- The crystal vibrates sinusoidally after electrical excitation has ended (resonate)
  - Resonant frequency $f=c/2d$ (d=thickness)
  - The damping material damps the vibration after 3-5 cycles
- When the diameter D of the surface is much larger than d, longitudinal waves are transmitted into the body
- The crystal is shaped into a disk or rectangle, with either flat or concave surface

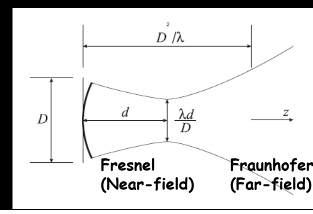
Matching Layer(s)

- To provide acoustic coupling between the crystal and patient skin and to protect surface of the crystal
- Z of PZT (Z_T) is ~15 times greater than Z of tissue (Z_L)
  - Placing crystal directly over skin would result a large amount of energy be reflected back from the boundary
    - » $R = |(Z_L - Z_T)/(Z_L + Z_T)| \sim 1$
- Matching layer
  - layer thickness = $\lambda/4$
  - $Z_I = \sqrt{(Z_T Z_L)}$
  - Maximize energy transfer into the body
- Problems: Finding material with exact Z_l value

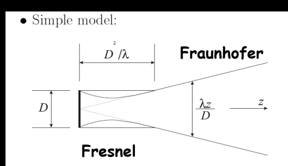


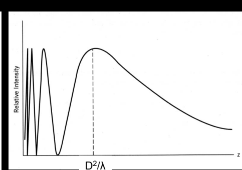
Ultrasound beam properties

- Beam focusing can be accomplished by
  - Using an element with a curved surface
  - Placing a concave lens in front of the transducer
  - Using a transducer array



Flat (Piston) Plate Transducer



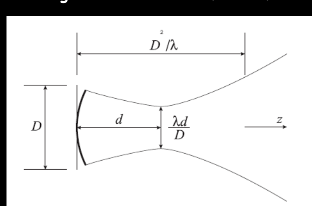


Beam Properties of a Piston Transducer

- At border of the beam width, the signal strength drops by a factor of 2, compared to the strength on the z-axis
- Beam width determines the imaging resolution (lateral resolution).
- Smaller D is good only before far field
- D=1~5 cm in practice, very poor lateral resolution
- Focused plate is used to produce narrow beam

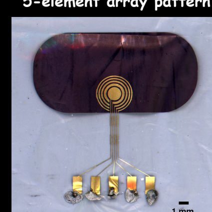
Focused Transducer

- Beam focusing can be accomplished by
  - Using a crystal with a curved surface
  - Placing a concave lens in front of the crystal

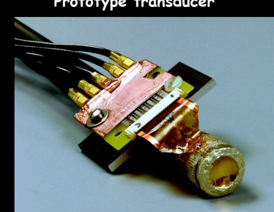


40-MHz annular array transducers for dynamic focusing

5-element array pattern



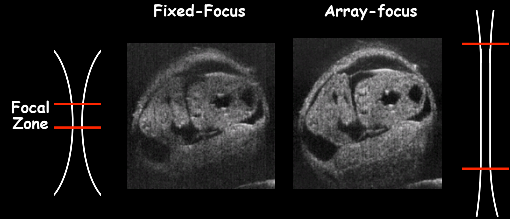
Prototype transducer



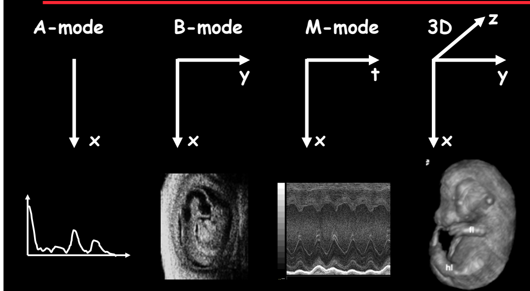
Ketterling et al, IEEE Trans UFFC 2005

Annular array transducer improves focusing in depth

E11.5 Mouse Embryo

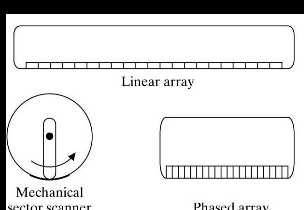


Ultrasound Scan Modes



B-mode Scanner Types

- B-mode scanners use multiple transducers



Transducer Array

- With a single element, mechanical steering of the beam is needed to produce a 2D image
- Practical systems today use an array of small piezoelectric elements
  - Allow electronic steering and focusing of the beam to optimize the lateral resolution

Array types

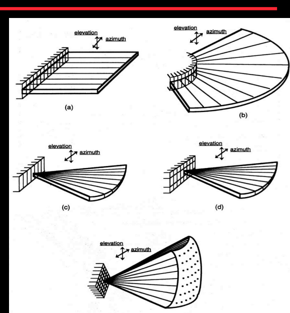
a) Linear Sequential (switched)
~1 cm x 10-15 cm, up to 512 elements

b) Curvilinear
similar to (a), wider field of view

c) Linear Phased
up to 128 elements, small footprint → cardiac imaging

d) 1.5D Array
3-9 elements in elevation allow for focusing

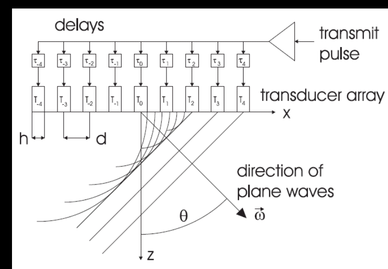
e) 2D Phased
Focusing, steering in both dimensions



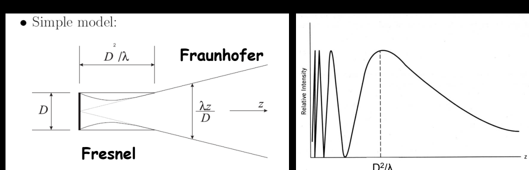
Phased Arrays

- Phased array:
  - Much smaller transducer elements than in linear array
  - Use electronic steering/focusing to vary transmit and receive beam directions

Beam Steering (Transmit)

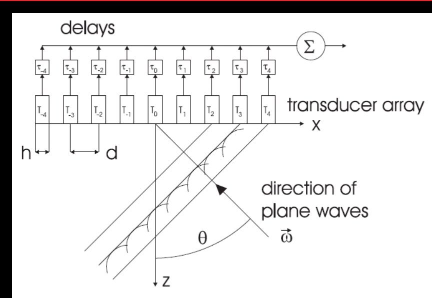


Flat (Piston) Plate Transducer



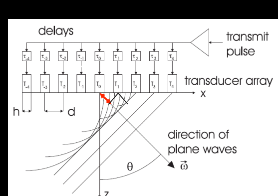
Array elements are flat pistons – operate in (Fraunhofer) farfield

Receive Beamforming



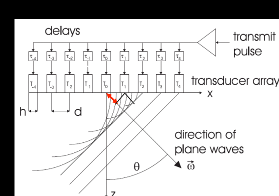
Delays for Steering

- Extra distance that T0 travels than T1:
  $\Delta d = d \sin\theta$
- For the wave from T1 to arrive at a point at the same time as T0, T1 should be delayed by
  $\Delta t = \Delta d/c = d \sin\theta/c$
- If T0 fires at t=0, Ti fires at
  $t_i = i\Delta t = id \sin\theta/c$



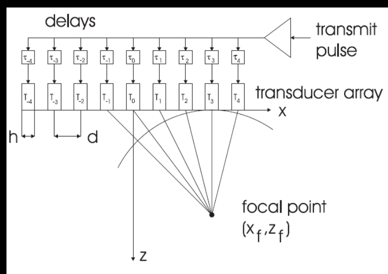
Grating lobes

- $t_i = i\Delta t = id \sin\theta/c$
- Steering direction is $\theta = \theta_0$ (Main lobe)
- Grating lobes (unwanted) in directions:
  $\sin\theta_g = \sin\theta_0 \pm j\lambda/d,\ j=1,2,\ldots$

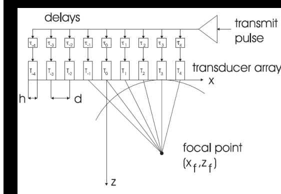


- Eg - $\theta_0 = 30°$, $d = 2\lambda$, then $\theta_g = \pm 90°, 0°$
  $\theta_0 = 30°$, $d = \lambda$, then $\theta_g = -30°$
- Avoid all grating lobes by choosing $d = \lambda/2$ (!)

Beam Focusing (Transmit)



Delays for Focusing



- Focal point at (x_f, z_f)
- T_i is at $(id, 0)$.
- Then range from T_i to focal point is:

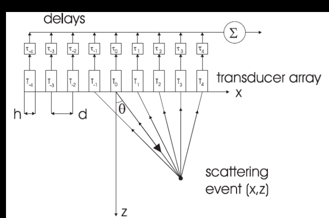
$$r_i = \sqrt{(id - x_f)^2 + z_f^2}$$

- Assume T_0 fires at $t = 0$. Then T_i fires at

$$t_i = \frac{r_0 - r_i}{c} = \frac{\sqrt{x_f^2 + z_f^2} - \sqrt{(id - x_f)^2 + z_f^2}}{c}$$

(Delays can be used to focus the beam on transmit and receive)

Receive Dynamic Focusing



T0 fires in direction θ, and all Ti's receive after a certain delay, so that they are all receiving signal from the same point at a particular time

Delays for Dynamic Focusing

- First consider a stationary scatterer at (x,z)
- Time for a wave to travel from T0 to the scatterer and then to Ti is
  $t_i = \{(x^2+z^2)^{1/2} + [(id-x)^2+z^2]^{1/2}\}/c$
- Time difference between arrival time at T0 and at Ti
  $\Delta t_i = t_0 - t_i$
- Desired time delay is a function of t:

$$\tau_i(t) = t - \frac{\sqrt{(id)^2 + (ct)^2 - 2ctid\sin\theta}}{c} + \frac{Nd}{c}$$

Practicalities of dynamic focusing

- Steer and focus the transmit beam in direction θ
- Focus the receive beam dynamically along that direction
- Increment steering direction to θ + Δθ
- Repeat for the new direction / image line

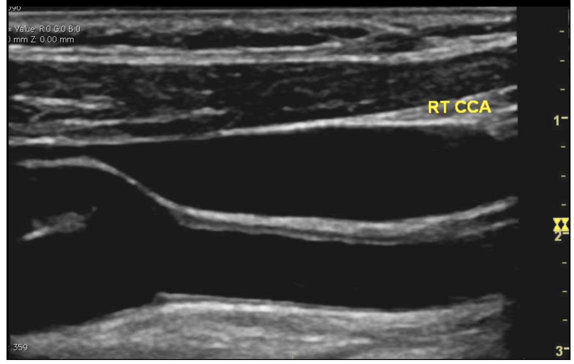
Steering and Focusing: Summary

- Beam steering and focusing are achieved simply by applying time delays on transmit and receive
- The time delays are computed using simple geometrical considerations, and assuming a single speed of sound
- These assumptions may not be correct, and may lead to artifacts

Clinical Applications

- Ultrasound is considered safe; instrument is less expensive and imaging is fast
- Clinical applications
  - Obstetrics and gynecology
    - » Widely used for fetus monitoring
  - Breast imaging
  - Musculoskeletal structure
  - Cardiac diseases
- Contrast agents

Carotid Artery



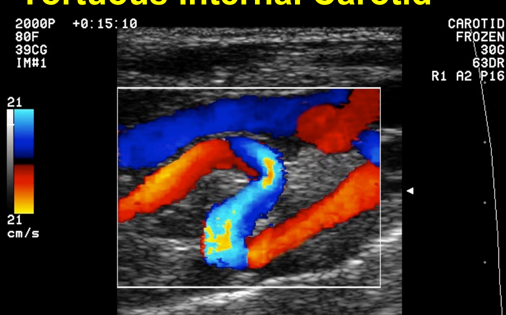
Plaque Morphology

Techniques in Noninvasive Vascular Diagnosis-3rd Ed., Rob Daigle, Summer Publishing LLC, Copyright 2009

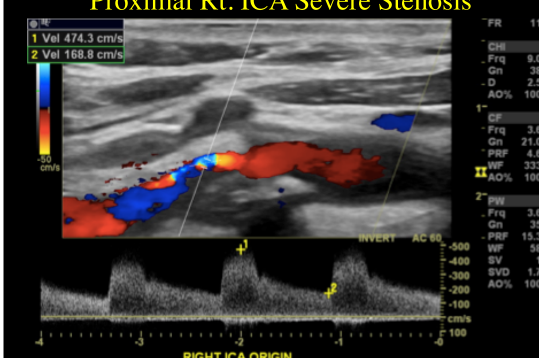
Plaque Morphology

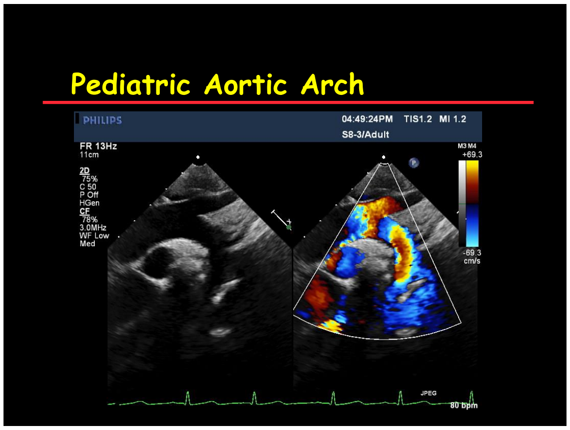
Techniques in Noninvasive Vascular Diagnosis-3rd Ed., Rob Daigle, Summer Publishing LLC, Copyright 2009

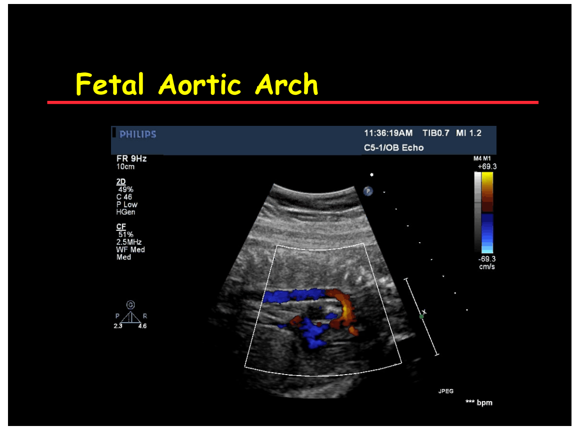
Tortuous Internal Carotid

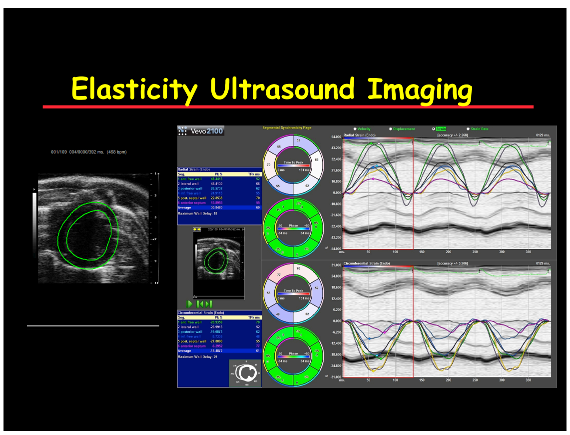


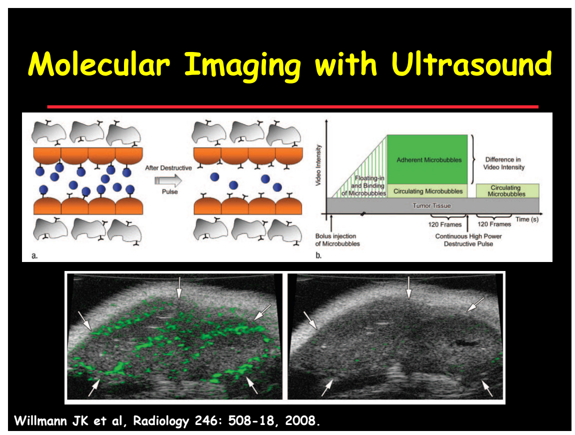
Proximal Rt. ICA Severe Stenosis

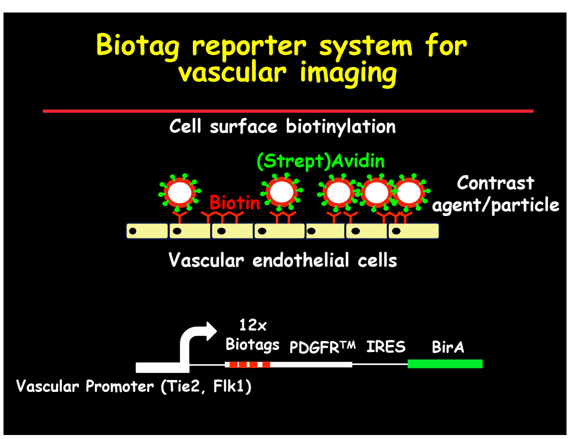


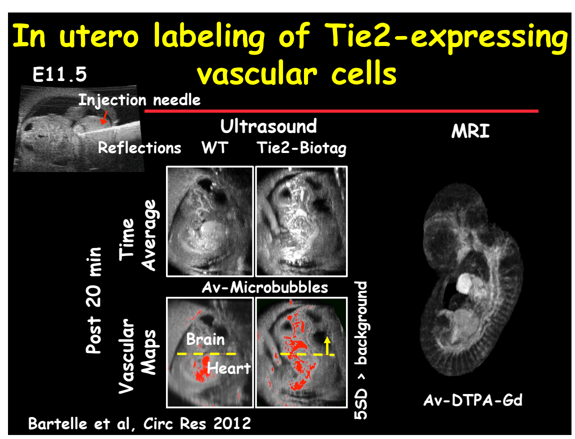

Pediatric Aortic Arch
PHILIPS
04:49:24PM TIS1.2 MI 1.2
S8-3/Adult
FR 13Hz
11cm
JPEG
80 bpm


Fetal Aortic Arch
PHILIPS
11:36:19AM TIB0.7 MI 1.2
C5-1/OB Echo
FR 9Hz
10cm
JPEG
*** bpm

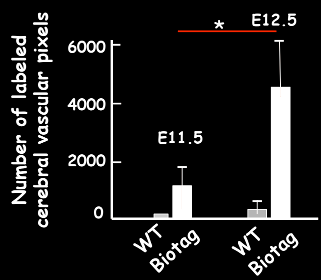

Elasticity Ultrasound Imaging
Vevo 2100


Molecular Imaging with Ultrasound
After Destructive Pulse
Video Intensity
Adherent Microbubbles
Difference in Video Intensity
Circulating Microbubbles
Tumor Tissue
Bolus injection of Microbubbles
120 Frames
Continuous High Power Destructive Pulse
Time (s)
a.
b.
Willmann JK et al, Radiology 246: 508-18, 2008.


Biotag reporter system for vascular imaging
Cell surface biotinylation
(Strept)Avidin
Biotin
Contrast agent/particle
Vascular endothelial cells
12x Biotags
PDGFR TM
IRES
BirA
Vascular Promoter (Tie2, Flk1)


In utero labeling of Tie2-expressing vascular cells
E11.5
Injection needle
Reflections
Ultrasound
WT
Tie2-Biotag
MRI
Post 20 min
Time Average
Av-Microbubbles
Vascular Maps
Brain
Heart
5SD > background
Av-DTPA-Gd
Bartelle et al, Circ Res 2012

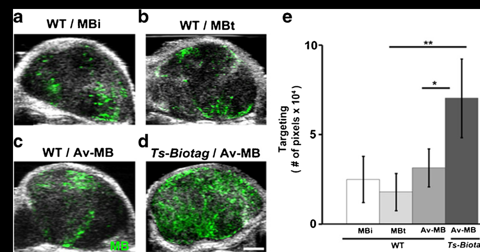
Biotag mice can be used to analyze changes in Tie2 expression in utero



In vivo analysis of Tie2 expression in good agreement with histology / immunostaining

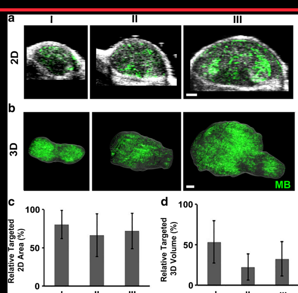
Bartelle et al, Circ Res 2012

Analysis of Tie2 expression in mouse melanoma tumors



Suero-Abreu et al, Mol Imaging Biol 2016

Analysis of Tie2 expression in mouse melanoma tumors



Suero-Abreu et al, Mol Imaging Biol 2016

Homework

- Reading:
  - Prince and Links, Medical Imaging Signals and Systems, Chapter 11
- Problems:
  - P11.6
  - P11.10
  - P11.14