

# EL736 Communications Networks II: Design and Algorithms

Class11: Multi-Hour and Multi-Layer  
Network Design  
12/05/2007

# Outline

- Multi-Hour Network Modeling & Design
  - uncapacitated
  - capacitated
  - robust routing
- Multi-Layer Networks
  - modeling
  - dimensioning
  - restoration

# Time-of-Day Effect

- ❑ Traffic demand varies during hours of a day
- ❑ Variations not synchronized

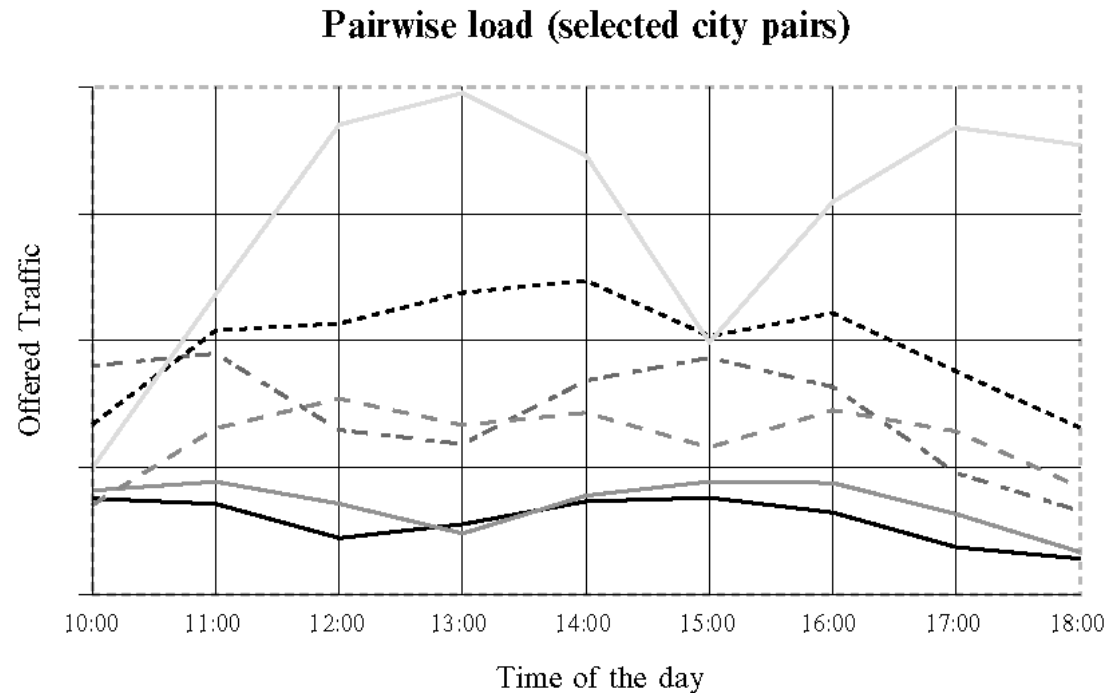


FIGURE 11.2 Traffic Variation for a Selected Set of City Pairs During the Day for a 10-Node Network Spanning Continental U.S. (Time is on Eastern Time Zone in U.S.)

# Multi-Hour Dimensioning

- ❑ how much capacities needed to handle demands at all times?
- ❑ rearrange routing when demand changes
- ❑ modular link dimensioning

## Modular Links, Multi-Hour, Rearrangeable

- indices

$d = 1, 2, \dots, D$  demands  
 $t = 1, 2, \dots, T$  traffic busy hours  
 $p = 1, 2, \dots, P_d$  allowable paths for flow realizing demand  $d$   
 $e = 1, 2, \dots, E$  links

- constants

$\delta_{edp}$  = 1, if link  $e$  belongs to path  $p$  realizing demand  $d$ , 0 otherwise  
 $h_{dt}$  volume of demand  $d$  at time  $t$   
 $\xi_e$  cost of one capacity module on link  $e$   
 $M$  size of the link capacity module

- variables

$x_{dpt}$  (non-negative) flow allocated to path  $p$  of demand  $d$   
at time  $t$  (continuous non-negative)  
 $y_e$  capacity of link  $e$  expressed in  
number of modules (non-negative integer)

- objective

minimize  $F = \sum_e \xi_e y_e$

- constraints

$\sum_p x_{dpt} = h_{dt}, \quad d = 1, 2, \dots, D \quad t = 1, 2, \dots, T$   
 $\sum_d \sum_p \delta_{edp} x_{dpt} \leq M y_e, \quad e = 1, 2, \dots, E \quad t = 1, 2, \dots, T.$

# Multi-Hour Dimensioning

- ❑ unsplittable flows: one path each demand
- ❑ non-rearrangeable routing: don't change routes over time

## Modular Links, Multi-Hour, Non-Rearrangeable, Unsplittable

- **indices**

$d = 1, 2, \dots, D$  demands

$t = 1, 2, \dots, T$  traffic busy hours

$p = 1, 2, \dots, P_d$  allowable paths for flow realizing demand  $d$

$e = 1, 2, \dots, E$  links

- **constants**

$\delta_{edp}$  = 1, if link  $e$  belongs to path  $p$  realizing demand  $d$ , 0 otherwise

$h_{dt}$  volume of demand  $d$  at time  $t$

$\xi_e$  cost of one capacity module on link  $e$

$M$  size of the link capacity module

- **variables**

$u_{dp}$  binary variable corresponding to the flow allocated to path  $p$  of demand  $d$

$y_e$  capacity of link  $e$  expressed in the number of modules (non-negative integer)

- **objective**

minimize  $F = \sum_e \xi_e y_e$

- **constraints**

$\sum_p u_{dp} = 1, \quad d = 1, 2, \dots, D$

$\sum_d h_{dt} \sum_p \delta_{edp} u_{dp} \leq M y_e, \quad e = 1, 2, \dots, E \quad t = 1, 2, \dots, T.$

# Multi-Hour Routing

- ❑ link capacity fixed
- ❑ recalculate routing for each time  $t$
- ❑ problem separable, optimal routing at each  $t$

## Multi-Hour, Rearrangeable, Capacitated

- **indices**

$d = 1, 2, \dots, D$  demands

$t = 1, 2, \dots, T$  time of the day index

$p = 1, 2, \dots, P_d$  allowable paths for flow realizing demand  $d$

$e = 1, 2, \dots, E$  links

- **constants**

$\delta_{edp}$  = 1, if link  $e$  belongs to path  $p$  realizing demand  $d$ , 0 otherwise

$h_{dt}$  volume of demand  $d$  at time  $t$

$\zeta_{dpt}$  unit routing cost on path  $p$  for demand  $d$   
in time window  $t$

$c_e$  capacity of link  $e$

- **variables**

$x_{dpt}$  flow allocated to path  $p$  of demand  $d$  at  
time  $t$  (continuous non-negative)

- **objective**

minimize  $F = \sum_d \sum_p \zeta_{dpt} x_{dpt}$

- **constraints**

$\sum_p x_{dpt} = h_{dt}, \quad d = 1, 2, \dots, D \quad t = 1, 2, \dots, T$

$\sum_d \sum_p \delta_{edp} x_{dpt} \leq c_e, \quad e = 1, 2, \dots, E \quad t = 1, 2, \dots, T.$

# Extension: robust routing under with multiple Traffic Matrices (TM)

## □ multiple Traffic Matrices

- **dynamic traffic:** demands between routing update period
- **estimation error:** possible traffic demands

## □ Robust routing: single set of routes achieving good performance under all possible TMs

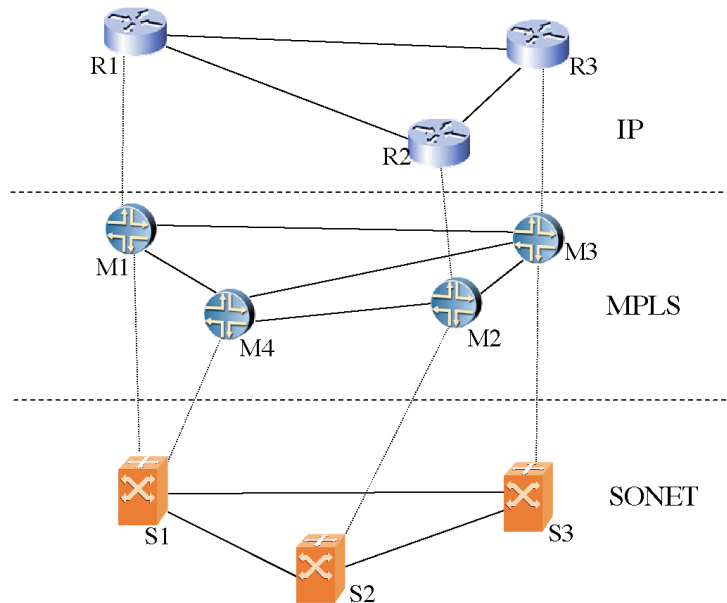
- routing reconfiguration too expensive
- routing: link-path, node-link, destination based, link weight based
- performance measure
  - good average performance
  - bounded worst-case performance
  - trade-off between two

## □ References

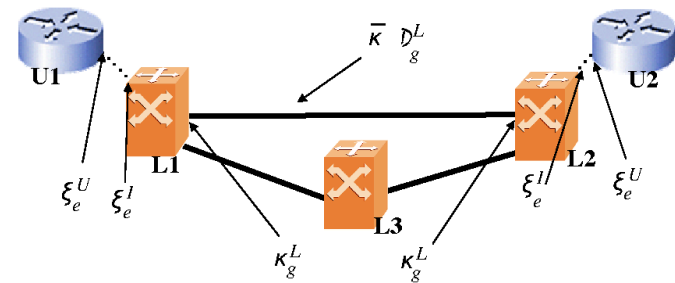
- "On Optimal Routing with Multiple Traffic Matrices",  
[http://eeweb.poly.edu/faculty/yongliu/docs/Zhang04\\_OptRoutingMultiTms.pdf](http://eeweb.poly.edu/faculty/yongliu/docs/Zhang04_OptRoutingMultiTms.pdf)
- "Optimal Routing with Multiple Traffic Matrices: Tradeoff between Average Case and Worst Case Performance",  
[ftp://gaia.cs.umass.edu/pub/Zhang05\\_tradeofftr.pdf](ftp://gaia.cs.umass.edu/pub/Zhang05_tradeofftr.pdf)

# Multi-Layer Networks

- ❑ Traffic vs. Transport Networks
- ❑ Technology Example



- ❑ Cost Component
  - cross-layer connection
  - physical connection





# Dimensioning at two Resource Layers

- ❑ demand layer
  - demand between pairs of users
  - to be carried by traffic network
- ❑ traffic network layer
  - set of logical links
  - realize each demand through flow allocation
  - capacity of each link realized by transport layer
- ❑ transport network layer
  - set of physical links
  - realize each logical link capacity through flow allocation
- ❑ **dimensioning**: how much capacity needed on each logical/physical link?

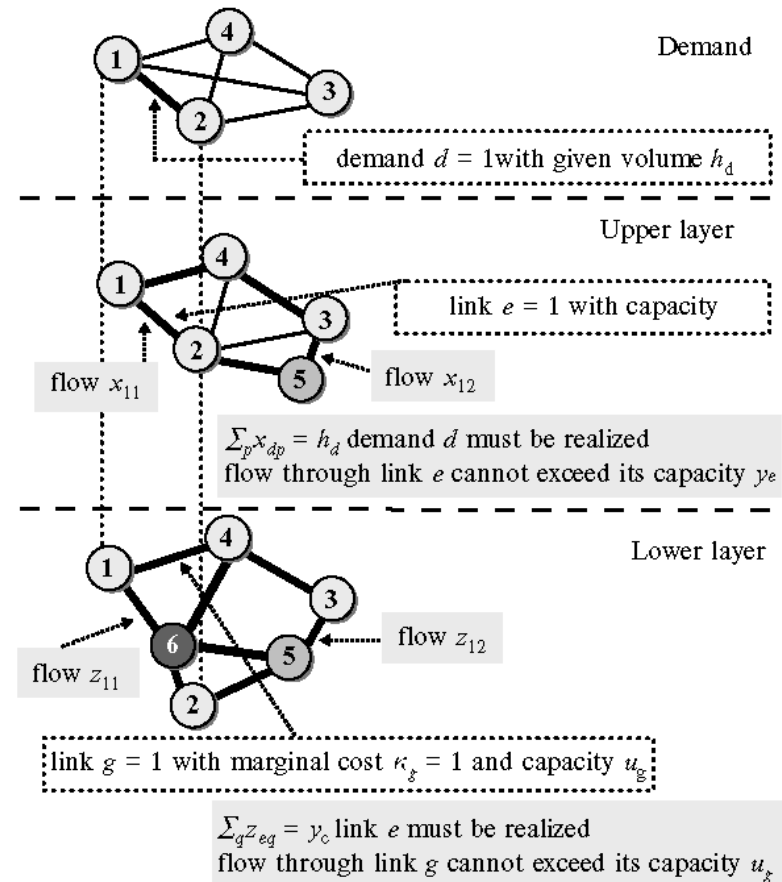


FIGURE 12.4 Two Resource Layer Network Example

# Two-Layer Dimensioning (continuous case)

- indices

$d = 1, 2, \dots, D$  demands  
 $p = 1, 2, \dots, P_d$  candidate paths in upper layer for flows realizing demand  $d$   
 $e = 1, 2, \dots, E$  links of upper layer  
 $q = 1, 2, \dots, Q_e$  candidate paths in lower layer for flows realizing link  $e$   
 $g = 1, 2, \dots, G$  links of lower layer

- constants

$h_d$  volume of demand  $d$   
 $\delta_{edp}$  = 1 if link  $e$  of upper layer belongs to path  $p$  realizing demand  $d$ ;  
 0, otherwise  
 $\xi_e$  unit cost of link  $e$  of upper layer  
 $\gamma_{geq}$  = 1 if link  $g$  of lower layer belongs to path  $q$  realizing link  $e$  of upper layer; 0, otherwise  
 $\kappa_g$  unit cost of link  $g$  of lower layer

- variables

$x_{dp}$  (non-negative continuous) flow allocated to path  $p$  realizing volume of demand  $d$   
 $y_e$  (non-negative continuous) capacity of upper layer link  $e$   
 $z_{eq}$  (non-negative continuous) flow allocated to path  $q$  realizing capacity of link  $e$   
 $u_g$  (non-negative continuous) capacity of lower layer link  $g$

sion August 2005 © John Wiley & Sons, Inc. *Engineering Optimization and Computer Networks* – p.5/52

- objective

$$\text{minimize } F = \sum_e \xi_e y_e + \sum_g \kappa_g u_g$$

- constraints

$$\sum_p x_{dp} = h_d, \quad d = 1, 2, \dots, D$$

$$\sum_d \sum_p \delta_{edp} x_{dp} \leq y_e, \quad e = 1, 2, \dots, E$$

$$\sum_q z_{eq} = y_e, \quad e = 1, 2, \dots, E$$

$$\sum_e \sum_q \gamma_{geq} z_{eq} \leq u_g, \quad g = 1, 2, \dots, G.$$

# Two-Layer Dimensioning (continuous/Integral)

- indices

$d = 1, 2, \dots, D$  demands  
 $p = 1, 2, \dots, P_d$  candidate paths in upper layer for flows realizing demand  $d$   
 $e = 1, 2, \dots, E$  links of upper layer  
 $q = 1, 2, \dots, Q_e$  candidate paths in lower layer for flows realizing link  $e$   
 $g = 1, 2, \dots, G$  links of lower layer

- constants

$h_d$  volume of demand  $d$   
 $\delta_{edp}$  = 1 if link  $e$  of upper layer belongs to path  $p$  realizing demand  $d$ ; 0, otherwise  
 $M$  size of the link capacity module in upper layer  
 $\xi_e$  cost of one ( $M$ -module) capacity unit of link  $e$  of upper layer  
 $\gamma_{geq}$  = 1 if link  $g$  of lower layer belongs to path  $q$  realizing link  $e$  of upper layer; 0, otherwise  
 $N$  size of link capacity module in lower layer  
 $\kappa_g$  cost of one ( $N$ -module) capacity unit of link  $g$  of lower layer

- variables

$x_{dp}$  (non-negative *continuous*) flow allocated to path  $p$  realizing volume of demand  $d$   
 $y_e$  (non-negative integral)  $M$ -module capacity of upper layer link  $e$   
 $z_{eq}$  (non-negative integral) flow allocated to path  $q$  realizing capacity of link  $e$   
 $u_g$  (non-negative integral) capacity of lower layer link  $g$

- objective

$$\text{minimize } F = \sum_e \xi_e y_e + \sum_g \kappa_g u_g$$

- constraints

$$\sum_p x_{dp} = h_d, \quad d = 1, 2, \dots, D$$

$$\sum_d \sum_p \delta_{edp} x_{dp} \leq M y_e, \quad e = 1, 2, \dots, E$$

$$\sum_q z_{eq} = y_e, \quad e = 1, 2, \dots, E$$

$$\sum_e M \sum_q \gamma_{geq} z_{eq} \leq N u_g, \quad g = 1, 2, \dots, G.$$

# Allocation with Two Layers of Resources

- ❑ lower layer capacities fixed
- ❑ upper layer capacities variable

*LP: A/2L/CF/BR/CC*

**Link-Path Formulation**

**Two-Layer Allocation Problem**

**indices**

- $d = 1, 2, \dots, D$  demands
- $p = 1, 2, \dots, P_d$  candidate paths in upper layer for demand  $d$
- $e = 1, 2, \dots, E$  links of upper layer
- $q = 1, 2, \dots, Q_e$  candidate paths in lower layer for flows realizing link  $e$
- $g = 1, 2, \dots, G$  links of lower layer

**constants**

- $h_d$  volume of demand  $d$
- $\delta_{edp} = 1$  if link  $e$  of upper layer belongs to path  $p$  realizing demand  $d$ ; 0, otherwise
- $\gamma_{geq} = 1$  if link  $g$  of lower layer belongs to path  $q$  realizing link  $e$  of upper layer; 0, otherwise
- $c_g$  capacity of lower layer link  $g$

**variables** (all non-negative continuous)

- $x_{dp}$  flow allocated to path  $p$  realizing volume of demand  $d$
- $y_e$  capacity of upper layer link  $e$
- $z_{eq}$  flow allocated to path  $q$  realizing capacity of link  $e$

**constraints**

$$\sum_p x_{dp} = h_d, \quad d = 1, 2, \dots, D \quad (12.1.7a)$$

$$\sum_d \sum_p \delta_{edp} x_{dp} \leq y_e, \quad e = 1, 2, \dots, E \quad (12.1.7b)$$

$$\sum_q z_{eq} = y_e, \quad e = 1, 2, \dots, E \quad (12.1.7c)$$

$$\sum_e \sum_q \gamma_{geq} z_{eq} \leq c_g, \quad g = 1, 2, \dots, G. \quad (12.1.7d)$$

# Two-Layer Mixed Dimensioning Allocation Problem

- ❑ lower layer capacities fixed
- ❑ upper layer link cost, lower layer routing cost

- **constants**

$h_d$	volume of demand $d$
$\delta_{edp}$	= 1 if link $e$ of upper layer belongs to path $p$ realizing demand $d$ ; 0, otherwise
$\gamma_{geq}$	= 1 if link $g$ of lower layer belongs to path $q$ realizing link $e$ of upper layer; 0, otherwise
$c_g$	capacity of lower layer link $g$
$M$	size of the link capacity module in upper layer
$\xi_e$	cost of one ( $M$ -module) capacity unit of link $e$ of upper layer
$\zeta_{eq}$	unit routing cost in the lower layer

- **variables**

$x_{dp}$	(non-negative continuous) flow allocated to path $p$ realizing volume of demand $d$
$y_e$	(non-negative integral) capacity of upper layer link $e$
$z_{eq}$	(non-negative integral) flow allocated to path $q$ realizing capacity of link $e$

August 2005 [http://www.ics.forth.gr/~dimitris/papers/Two-Layer-Dimensioning-Problem.pdf](#) Journal of Communication and Computer Networks – p.16/52

- **objective**

$$\text{minimize } \sum_e \xi_e y_e + \sum_e \sum_q \zeta_{eq} z_{eq}$$

- **constraints**

$$\begin{aligned} \sum_p x_{dp} &= h_d, \quad d = 1, 2, \dots, D \\ \sum_d \sum_p \delta_{edp} x_{dp} &\leq M y_e, \quad e = 1, 2, \dots, E \\ \sum_q z_{eq} &= y_e, \quad e = 1, 2, \dots, E \\ \sum_e \sum_q \gamma_{geq} z_{eq} &\leq c_g, \quad g = 1, 2, \dots, G. \end{aligned}$$

# Extension to More than Two Layers

- ❑ Example: IP/MPLS/SONET
- ❑ link at layer  $k+1$  is demand for layer  $k$
- ❑ demand considered the top layer
- ❑ joint dimensioning across all layers
- ❑ generalized shortest path allocation rule
  - at layer  $k$ , allocate a layer  $k+1$  demand (link  $l^{k+1}$ ) to its cheapest path  $p^k$
  - set link weight at layer  $k+1$  for  $l^{k+1}$  using length of  $p^k$  at layer  $k$
  - repeat until find the shortest paths for all demands

# Extension: joint optimal routing and capacity design in upper layer

- ❑ routing: given demands, link capacities, find the best flow allocation
- ❑ capacity allocation normally done in coarser time scale
- ❑ exception in wireless/sensor network
  - no well-defined link capacity
  - links from same node share resource: spectrum, power, timeslot
  - link capacities be adjusted along with routing
- ❑ joint optimization of rate control, routing and resource allocation
  - reference: "A Distributed Algorithm for Joint Sensing and Routing in Wireless Networks with Non-Steerable Directional Antennas", [ftp://gaia.cs.umass.edu/pub/Zhang06\\_jointopt\\_tr0612.pdf](ftp://gaia.cs.umass.edu/pub/Zhang06_jointopt_tr0612.pdf)

# Multi-Layer Networks for Restoration Design

- Upon failures, path restorations can be done
  - in both upper and lower layers
  - low layer only
  - upper layer only
- Example: IP/SONET
  - upon failure: IP Re-routing/SONET reconfiguration
  - time-scale difference
  - transit loss of link capacity in IP layer
  - transit loss of packets for demands

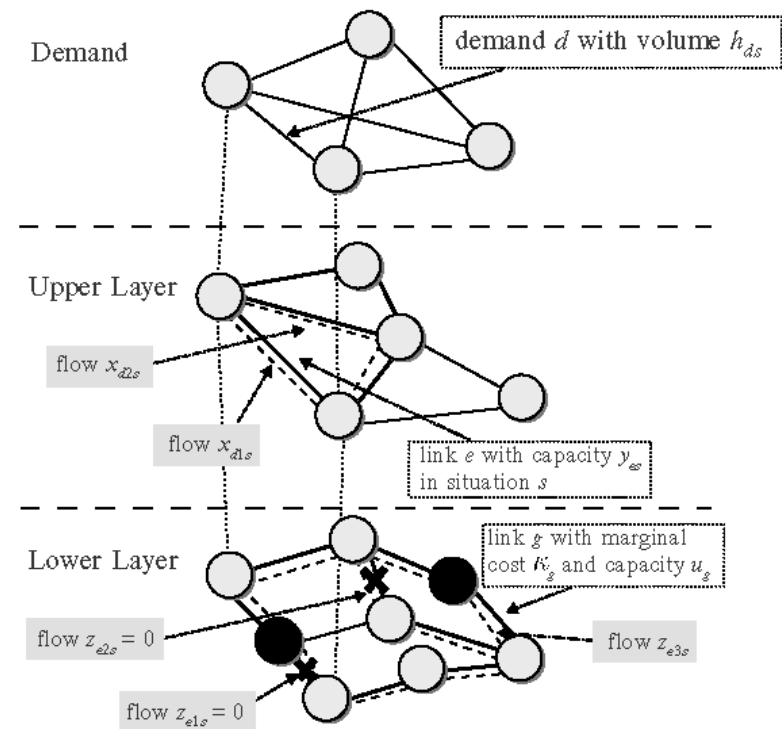


FIGURE 12.5 Two-Layer Networks with Failures



# Two-Layer Restoration Dimensioning with Unrestricted Flow Reconfiguration

- ❑ capacity dimensioning to handle all possible failure states
- ❑ arbitrary flow reconfiguration at both layers

## indices

$d = 1, 2, \dots, D$	demands
$p = 1, 2, \dots, P_d$	candidate paths in upper layer for flows realizing demand $d$
$e = 1, 2, \dots, E$	links of upper layer
$q = 1, 2, \dots, Q_e$	candidate paths in lower layer for flows realizing link $e$
$g = 1, 2, \dots, G$	links of lower layer
$v = 1, 2, \dots, V$	nodes of upper layer
$s = 1, 2, \dots, S$	failure-demand states (situations) (including the normal state)

## constants

$h_d$	volume of demand $d$
$a_{ve}$	= 1 if link $e$ is incident with node $v$ ; 0, otherwise
$\delta_{edp}$	= 1 if link $e$ of upper layer belongs to path $p$ realizing demand $d$ ; 0, otherwise
$\gamma_{geq}$	= 1 if link $g$ of lower layer belongs to path $q$ realizing link $e$ of upper layer; 0, otherwise
$\varsigma_v$	unit cost of the capacity of node $v$ of upper layer (termination cost and switching cost)
$\kappa_g$	unit cost of link $g$ of lower layer
$\chi_{ds}$	demand coefficient of demand $d$ in state $s$ , $h_{ds} = \chi_{ds} h_d$
$\beta_{vs}$	binary availability coefficient of node $v$ of upper layer in state $s$ ( $\beta_{vs} \in \{0, 1\}$ )
$\alpha_{gs}$	fractional availability coefficient of link $g$ of lower layer in state $s$ ( $0 \leq \alpha_{gs} \leq 1$ )

# Two-Layer Restoration Dimensioning with Unrestricted Flow Reconfiguration

- **variables** (all variables are continuous and non-negative)

$x_{dps}$  flow allocated to path  $p$  of demand  $d$  in state  $s$

$Y_v$  capacity of node  $v$  of upper layer (state-independent)

$y_{es}$  capacity of link  $e$  in state  $s$  (situation-dependent)

$z_{eqs}$  flow allocated to path  $q$  realizing capacity of link  $e$  in state  $s$

$u_g$  capacity of link  $g$

- **objective**

$$\text{minimize } F = \sum_g \kappa_g u_g + \sum_v \varsigma_v Y_v$$

- **constraints**

$$\sum_p x_{dps} = h_{ds}, \quad d = 1, 2, \dots, D \quad s = 1, 2, \dots, S$$

$$\sum_d \sum_p \delta_{edp} x_{dps} \leq y_{es}, \quad e = 1, 2, \dots, E \quad s = 1, 2, \dots, S$$

$$\sum_e a_{ve} y_{es} \leq \beta_v Y_v, \quad v = 1, 2, \dots, V \quad s = 1, 2, \dots, S$$

$$\sum_q z_{eqs} = y_{es}, \quad e = 1, 2, \dots, E \quad s = 1, 2, \dots, S$$

$$\sum_e \sum_q \gamma_{geq} z_{eqs} \leq \alpha_{gs} u_g, \quad g = 1, 2, \dots, G \quad s = 1, 2, \dots, S.$$

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Routing, Flow, and Capacity Design in Communication and Comput

# Restoration Dimensioning with reconfiguration only at lower layer

- ❑ upper layer link capacities and flows required to be same under any failure state (no rerouting allowed)
- ❑ lower layer flow reconfigurable

**additional constants**

$H_d$   $\max\{h_{ds}, s = 1, 2, \dots, S\}$  maximal value of demand  $d$

**variables** (all variables are continuous and non-negative)

$x_{dp}$  flow allocated to path  $p$  of demand  $d$  in all states

$y_e$  capacity of link  $e$  in all states

$z_{eqs}$  flow allocated to path  $q$  realizing capacity of link  $e$  in state  $s$

$u_g$  capacity of link  $g$

**objective**

$$\text{minimize } F = \sum_g \kappa_g u_g \quad (12.2.4a)$$

**constraints**

$$\sum_p x_{dp} = H_d, \quad d = 1, 2, \dots, D \quad (12.2.4b)$$

$$\sum_d \sum_p \delta_{edp} x_{dp} \leq y_e, \quad e = 1, 2, \dots, E \quad (12.2.4c)$$

$$\sum_q z_{eqs} = y_e, \quad e = 1, 2, \dots, E \quad s = 1, 2, \dots, S \quad (12.2.4d)$$

$$\sum_e \sum_q \gamma_{geq} z_{eqs} \leq \alpha_{gs} u_g, \quad g = 1, 2, \dots, G \quad s = 1, 2, \dots, S. \quad (12.2.4e)$$

# Restoration Dimensioning with reconfiguration only at upper layer

- ❑ lower layer flows are not reconfigurable, lower layer path may not available after failure
- ❑ upper layer link capacities affected by failure, and flows can be reconfigured arbitrarily

**variables** (all variables are continuous and non-negative)

$x_{dps}$  flow allocated to path  $p$  of demand  $d$  in state  $s$

$y_{es}$  capacity of link  $e$  in state  $s$

$z_{eq}$  flow allocated to path  $q$  realizing capacity of link  $e$  in all state

$u_g$  capacity of link  $g$

**objective**

$$\text{minimize } F = \sum_g \kappa_g u_g \quad (12.2.5a)$$

**constraints**

$$\sum_p x_{dp} = h_{ds}, \quad d = 1, 2, \dots, D \quad s = 1, 2, \dots, S \quad (12.2.5b)$$

$$\sum_d \sum_p \delta_{edp} x_{dps} \leq y_{es}, \quad e = 1, 2, \dots, E \quad s = 1, 2, \dots, S \quad (12.2.5c)$$

$$\sum_q \theta_{eqs} z_{eq} \geq y_{es}, \quad e = 1, 2, \dots, E \quad s = 1, 2, \dots, S \quad (12.2.5d)$$

$$\sum_e \sum_q \gamma_{geq} z_{eq} \leq u_g, \quad g = 1, 2, \dots, G. \quad (12.2.5e)$$

# Extension: Overlay/P2P Networks

## □ Overlay Networks

- logical networks on top of physical networks
- improved end user performance
- new services:
  - Content distribution: Akamai
  - p2p file sharing: BitTorrent, EMule
  - Streaming/multicast: Skype/IPTV

## □ Overlay Network Design

- efficiency: topologies, routing, scheduling, rate control
- interaction with native IP networks

## □ Reference:

"On the Interaction Between Overlay Routing and Traffic Engineering",  
<http://eeweb.poly.edu/faculty/yongliu/docs/info05.pdf>

